Balancing on a Knife Edge While Doing Something Else

by Roy Featherstone

http://royfeatherstone.org

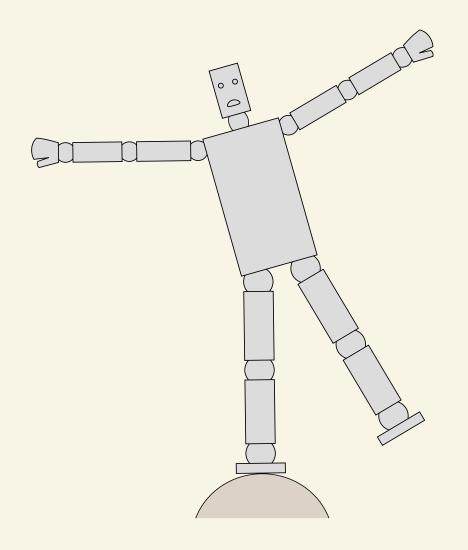
This seminar begins with a viewing of the following movie:

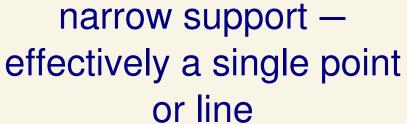
High Performance Balancing on a Narrow Support

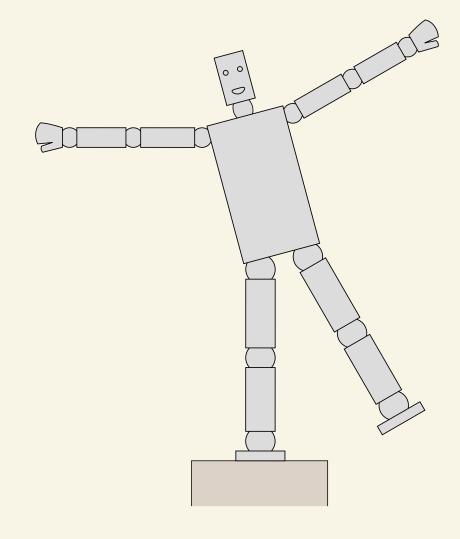
http://royfeatherstone.org/talks/icra2021rf.mp4

(clicking won't work, but copy and paste might)

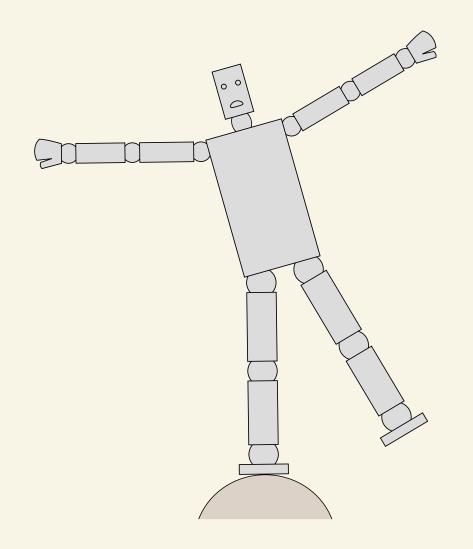
presented originally at ICRA 2021



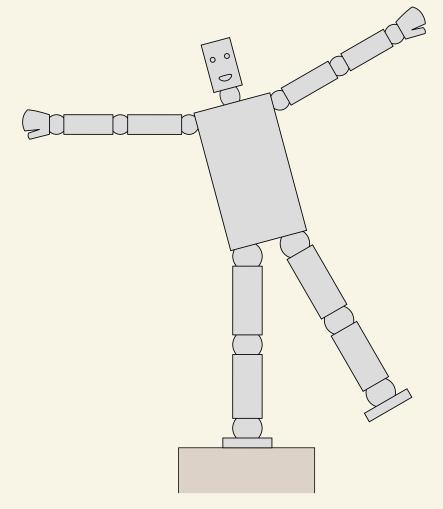




substantial polygon of support



dynamically unstable — must balance actively



statically stable as long as ground reaction force stays inside support polygon

High-Performance Balancing

Definition:

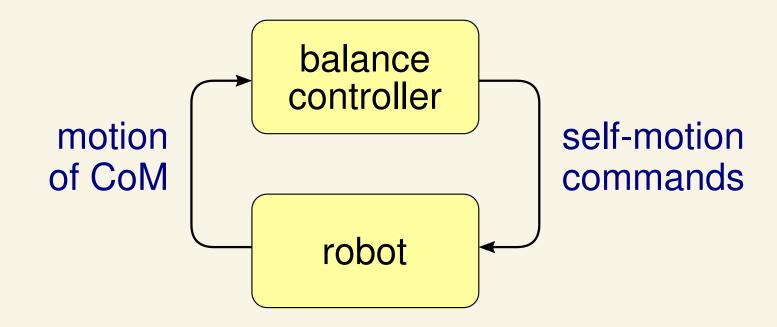
A robot is a high-performance balancer if it can

- accurately follow commands to make large, fast movements without losing its balance; and
- quickly recover from large balance disturbances

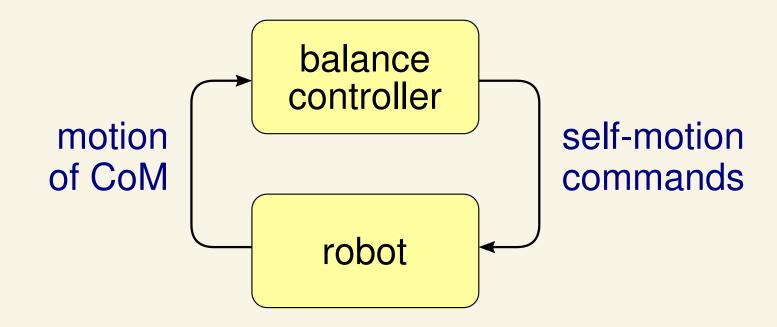
High-Performance Balancing

Our Approach:

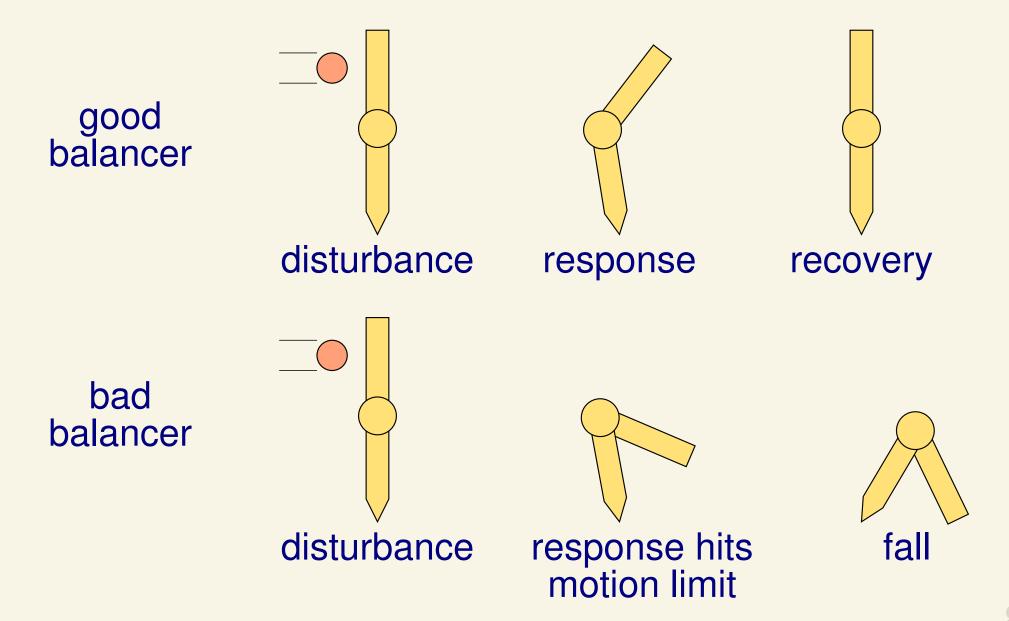
- Balancing is a physical activity, not just a control theory exercise;
 - so study the physics of balancing
- A robot's physical ability to balance is a property of the robot itself, not the control system;
 - so study what makes a robot good at balancing, and make your robot good by design.



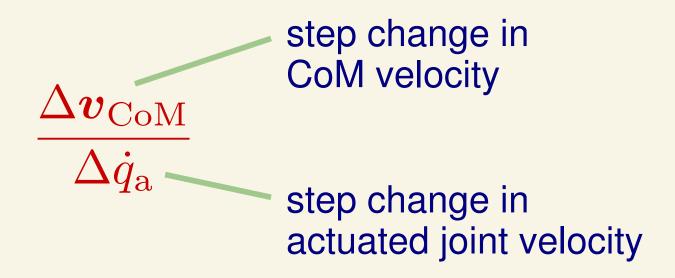
Balancing on a narrow support requires moving the robot's centre of mass (CoM) relative to the support by means of self motions (i.e., motions of the actuated joints).



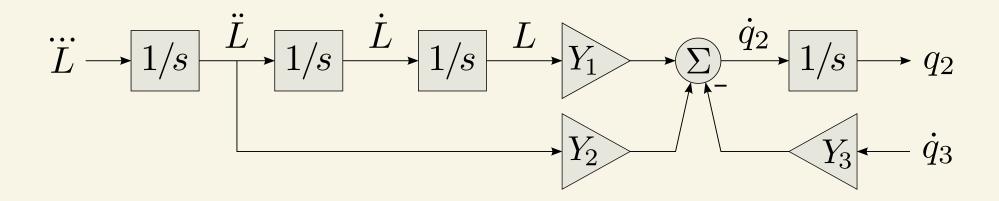
So a robot is *physically good at balancing* if a relatively small self motion causes a relatively large CoM motion.



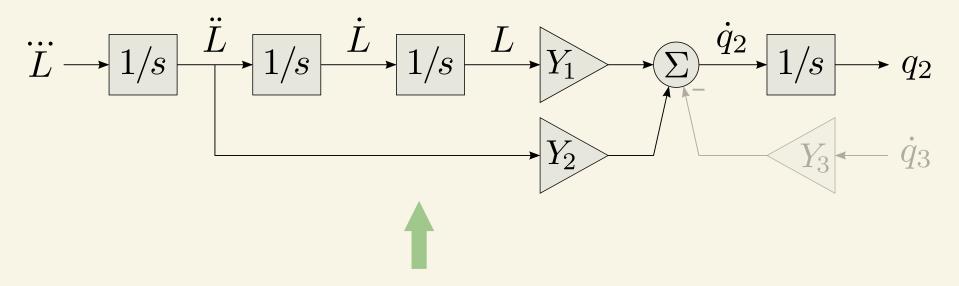
This leads to the idea of *velocity gain*:



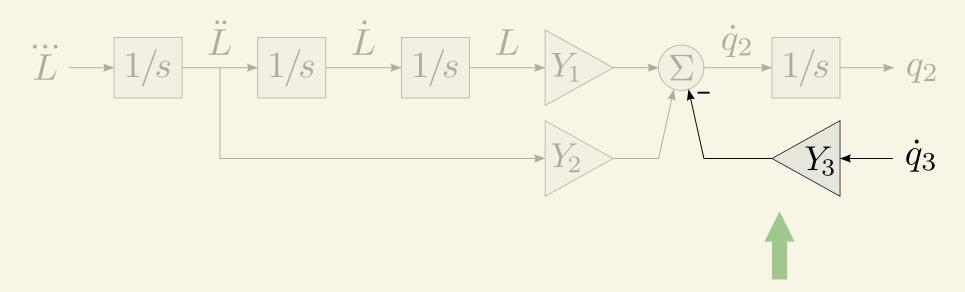
both caused by an impulse at the actuated joint



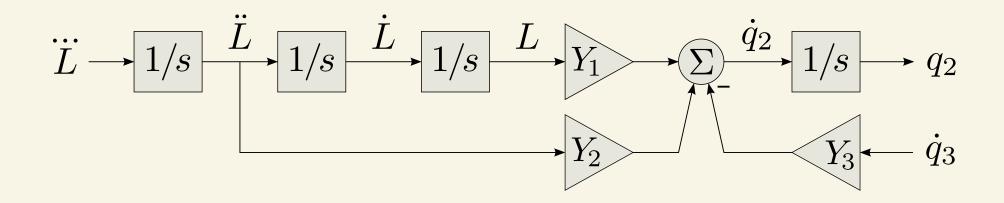
The physical process of balancing can be expressed in the form of this block diagram, which serves as the *plant* for the balance controller to control.



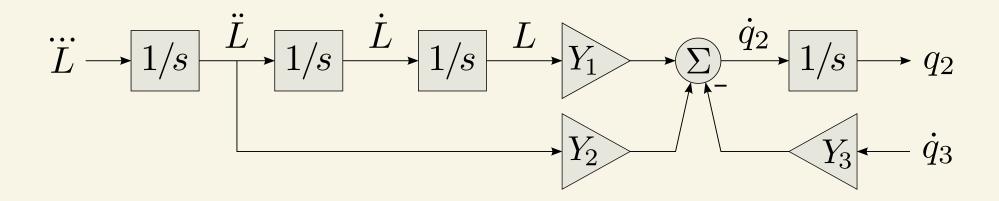
This portion is concerned with balancing



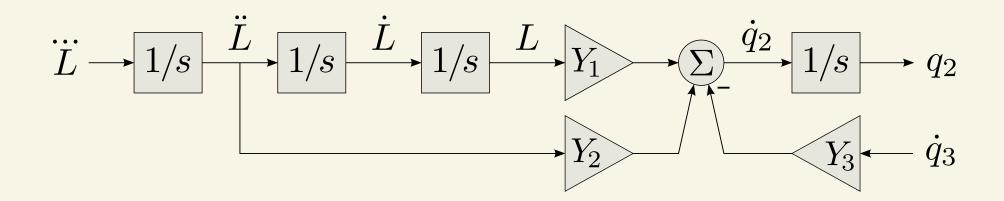
and this portion describes the disturbances caused by other motions.



- L angular momentum of the robot about the support
- q_1 variable describing the robot's angle relative to the ground (passive revolute joint)
- q_2 overloaded variable used both to balance and to follow motion commands
- q_3 all other position variables

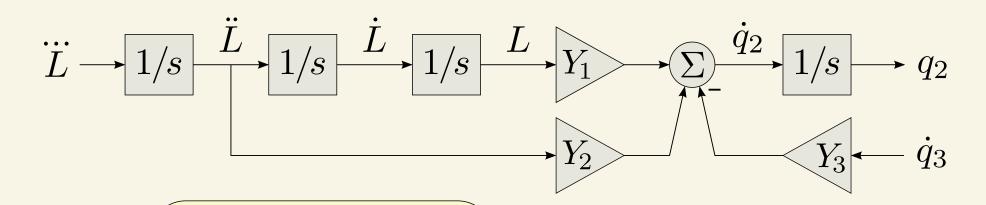


The balancing behaviour of the robot depends only on the two gains Y_1 and Y_2 which are easily calculated functions of the robot's configuration variables.



 Y_1 and Y_2 are functions of two easily measured physical properties of the robot:

- ullet the natural time constant of toppling, $T_{
 m c}$, and
- ullet the linear velocity gain of \dot{q}_2



the rate at which the robot begins to fall if proper q_2 is held constant

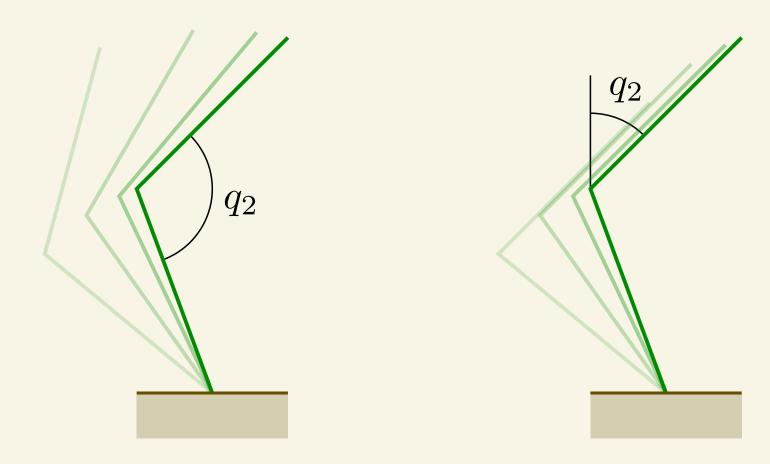
wo easily measured physical

- the natural time constant of toppling T and
- ullet the linear velocity gain of \dot{q}_2

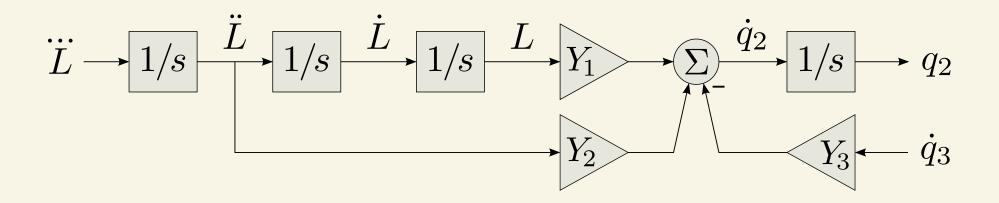
the step change in CoM velocity caused by a unit step change in \dot{q}_2

Different Ways to Fall

The time constant of toppling, T_c , is the rate at which the robot would start to fall if q_2 is held constant. It therefore depends on the definition of q_2 . Here are two examples:



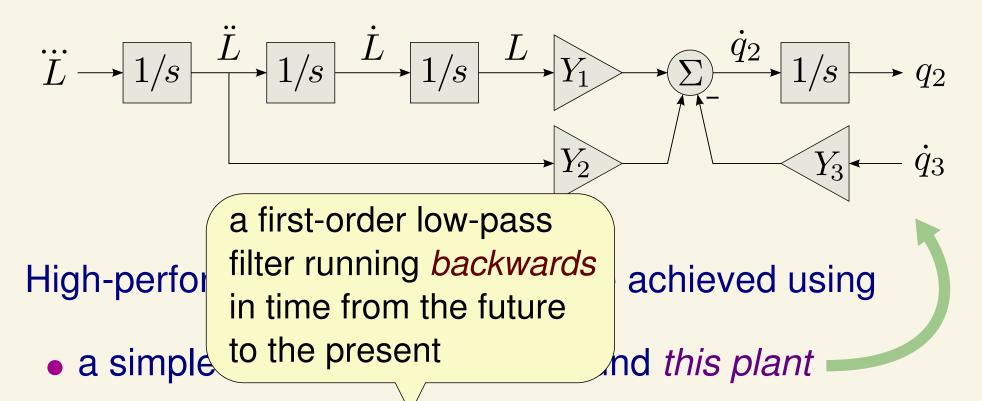
Simple Balance Control



High-performance balancing can be achieved using

- a simple control law closed around this plant
- and a simple acausal filter that implements
 leaning in anticipation of the balance disturbances
 that will be caused by commanded future motions.

Simple Balance Control



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The Acausal Filter

a first-order low-pass filter running backwards in time to cancel the non-minimum-phase response of the robot

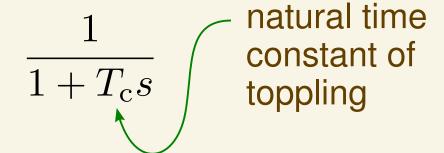
normal low-pass filter

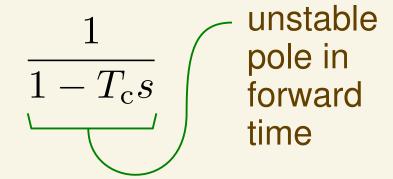


acausal low-pass filter

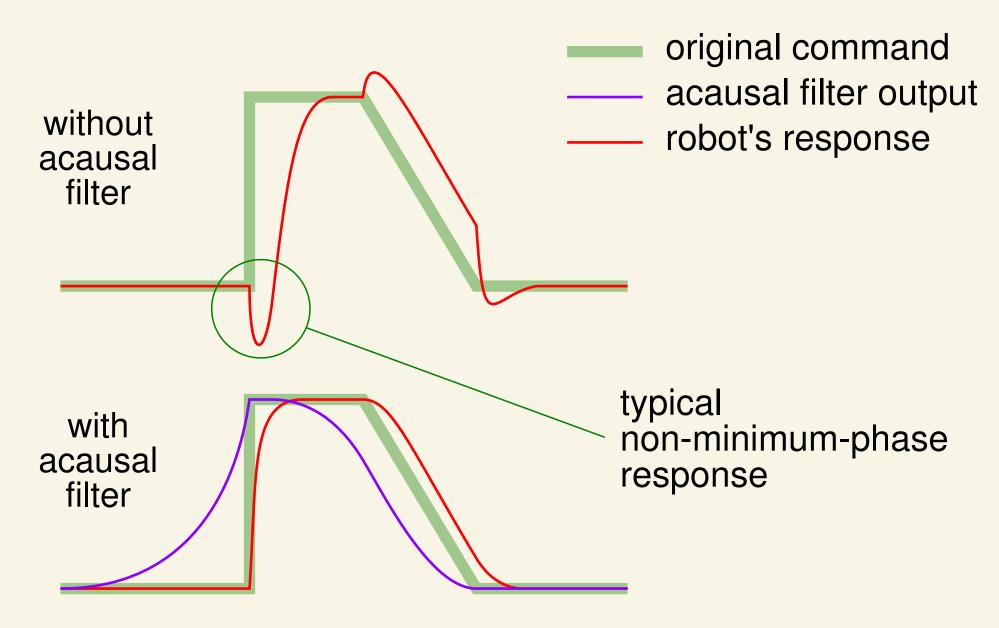


transfer function

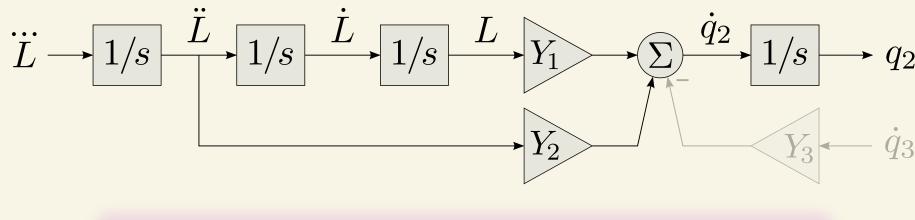




The Acausal Filter

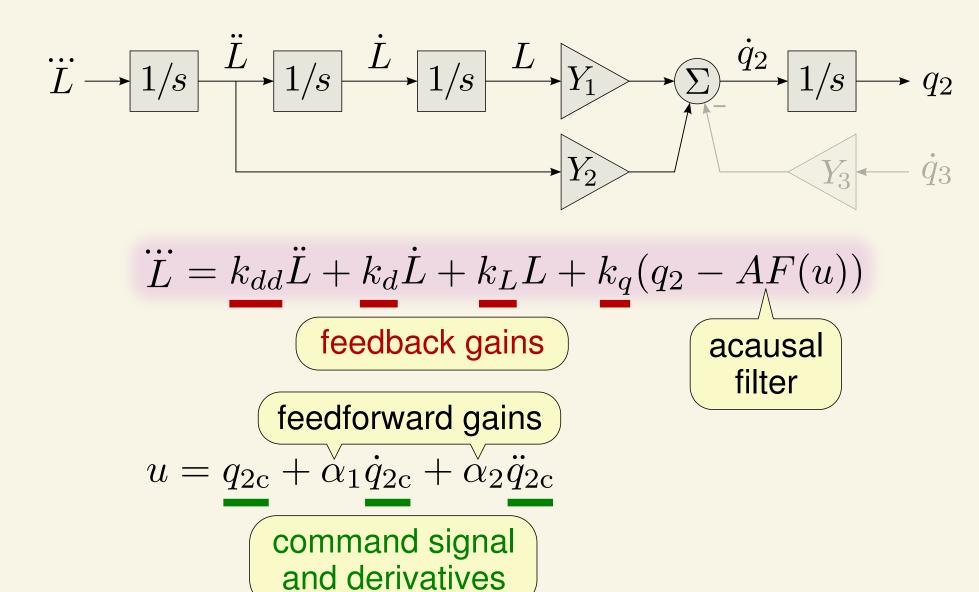


Balance Control Law



$$\ddot{L} = k_{dd}\ddot{L} + k_{d}\dot{L} + k_{L}L + k_{q}(q_2 - AF(u))$$

Balance Control Law



The seminar concludes with a viewing of the following movie:

Control of Absolute Motion While Balancing in 2D

http://royfeatherstone.org/talks/icar21.mp4

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presented originally at ICAR 2021