# Balancing on a Knife Edge While Doing Something Else

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This seminar begins with a viewing of the following movie:

## **High Performance Balancing on a Narrow Support**

#### http://royfeatherstone.org/talks/icra2021rf.mp4

(clicking won't work, but copy and paste might)

presented originally at ICRA 2021

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narrow support effectively a single point or line

substantial polygon of support



 $d$ ynamically unstable  $$ must balance actively

statically stable as long as ground reaction force stays inside support polygon

### High-Performance Balancing

Definition:

A robot is a high-performance balancer if it can

- accurately follow commands to make large, fast movements without losing its balance; and
- quickly recover from large balance disturbances

### High-Performance Balancing

Our Approach:

- 1. Balancing is a physical activity, not just a control theory exercise;
	- so study the *physics of balancing*
- A robot's physical ability to balance is a property of **2.**the robot itself, not the control system;
	- so study what makes a robot good at balancing, and make your robot *good by design*.



Balancing on a narrow support requires moving the robot's centre of mass (CoM) relative to the support by means of self motions (i.e., motions of the actuated joints).



So a robot is *physically good at balancing* if a relatively small self motion causes a relatively large CoM motion.



This leads to the idea of *velocity gain*:



both caused by an impulse at the actuated joint



The physical process of balancing can be expressed in the form of this block diagram, which serves as the *plant* for the balance controller to control.



This portion is concerned with balancing



and this portion describes the disturbances caused by other motions.



- angular momentum of the robot about the support  $L$
- variable describing the robot's angle relative to the  $\overline{q_1}$ ground (passive revolute joint)
- *overloaded* variable used *both* to balance *and* to  $q_2$ follow motion commands
- all other position variables $q_3$



The balancing behaviour of the robot depends only on the two gains  $Y_1$  and  $Y_2$  which are easily calculated functions of the robot's configuration variables.



 $Y_1$  and  $Y_2$  are functions of two easily measured physical properties of the robot:

- $\bullet$  the natural time constant of toppling,  $T_c$ , and
- the linear velocity gain of  $\dot{q}_2$



#### Different Ways to Fall

The time constant of toppling,  $T_c$ , is the rate at which the robot would start to fall if  $q_2$  is held constant. It therefore depends on the definition of  $q_2$ . Here are two examples:



#### Simple Balance Control



High-performance balancing can be achieved using

- a simple control law closed around *this plant*
- and a simple *acausal filter* that implements *leaning in anticipation* of the balance disturbances that will be caused by commanded future motions.

#### Simple Balance Control



and a simple *acausal filter* that implements *leaning in anticipation* of the balance disturbances that will be caused by commanded future motions.

#### The Acausal Filter

a first-order low-pass filter running backwards in time to cancel the non-minimum-phase response of the robot



#### The Acausal Filter



#### Balance Control Law



 $\dddot{L} = k_{dd}\ddot{L} + k_d\dot{L} + k_L L + k_q(q_2 - AF(u))$ 

#### Balance Control Law



The seminar concludes with a viewing of the following movie:

# **Control of Absolute Motion While Balancing in 2D**

http://royfeatherstone.org/talks/icar21.mp4

(clicking won't work, but copy and paste might)

presented originally at ICAR 2021